



**"Gheorghe Asachi" Technical University of Iasi, Romania**



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## OPTIMIZATION OF THE EVACUATION ROUTE IN CHEMICAL PLANTS BASED ON THE DEPTH-FIRST SEARCH ALGORITHM

**Ying Liu<sup>1,2</sup>, Zuoling You<sup>1</sup>, Fa Wang<sup>1</sup>, Yunrui Zhang<sup>1</sup>, Bo Zhang<sup>1,3\*</sup>**

<sup>1</sup>Department of Safety Science & Engineering, China University of Petroleum (East China), Qingdao 266580, P.R. China

<sup>2</sup>Dan F. Smith Department of Chemical Engineering, Lamar University, Beaumont, TX, 77710, USA

<sup>3</sup>Centre for offshore Engineering and Safety Technology (COEST), China University of Petroleum (East China), Qingdao 266580, P.R. China

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### Abstract

Optimal evacuation routes are crucial to protect workers' safety when accidental leakage of toxic gas occurs in chemical plants. However, the majority of route optimization focuses on the transport field and few on the evacuation routing optimization in chemical plants. This paper proposes a dynamic evacuation routing optimization method for chemical plants under toxic gas release scenarios. From the complete accident scenario set (CASS) built with wind fields and leakage sources, the leakage probability can be quantitatively represented. Based on the computational fluid dynamics (CFD) simulation, the consequences of toxic gas dispersion including the time-dependent concentration under different leakage scenarios can be obtained. Subsequently, considering the time-dependent toxic gas concentration and exposure time, the dynamic cumulative individual risk (CIR) can be calculated by applying the dynamic dose-response model (DDR). Then according to the simplified evacuation topology, the Depth First Search (DFS) algorithm is employed to define all evacuation routes connected with arcs. With the objective of minimizing CIR, an evacuation route optimization model is proposed and solved by MATLAB. Results demonstrate that the proposed method can hopefully minimize the CIR in chemical plants when they are facing toxic gas release and poisoning risks.

**Key words:** complete accident scenario set; computational fluid dynamics; Depth First Search; dynamic dose-response model; evacuation routing optimization

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### 1. Introduction

An appropriate evacuation route can reduce losses during evacuation when toxic gas releases in chemical plants (Xi et al., 2016), especially when shelter-in-place fails. Toxic gases usually exist in chemical plants, such as chlorine and ammonia, leakage of such gases may lead to multiple casualties (Li et al., 2012; Xiong et al., 2016; Zhang et al., 2017; Zhu et al., 2009). For example, an anhydrous ammonia release incident at the Millard Refrigerated Services, Alabama, on August 23, 2010, caused one employee injured during evacuation (CSB, 2015). Therefore, a proper evacuation pathway should be identified to reduce losses when gas leakage accidents occur in

chemical plants (Dou et al., 2019; Xiong et al., 2016; Zhou et al., 2008).

The evacuation routing optimization problem has aroused interest in many researchers since it is of vital significance to reduce losses when accidents happen (Aziz et al., 2017; Gai et al., 2018; Li, 2009; Liu et al., 2016). Various approaches are proposed and developed to handle routing optimization. In general, they are based on mathematical modeling, simulation, and soft computing (Liu et al., 2016; Zhang et al., 2013). New sights have been brought by soft computing, which is based on intelligent algorithms and effective to solve evacuation problems by stochastic programming methods. As for stochastic programming, appropriate measures are important in

\* Author to whom all correspondence should be addressed: e-mail: zhangbo@upc.edu.cn; Phone: +86-532-86983500-8707; Fax: +86-532-86983300

yielding the best evacuation plan (Yuan and Han, 2009). The number of optimization objectives varies with optimization targets. Setting the minimal evacuation time as objective, a modified Dijkstra algorithm is proposed to solve the optimization model (Yuan and Wang, 2008; Zheng et al., 2019). Improved algorithms based on heuristics are developed to solve multi-objective evacuation routing problems (Gai et al., 2017; Koca et al., 2018; Kou et al., 2013). In large-scale evacuation problems, such as the evacuation of the downtown population in big cities under terrorist attacks, gas leakage or natural disasters, the combinational explosion of routes will increase computation time significantly. Thus, heuristic algorithms are commonly applied to solve such problems (Li and Chen, 2012; Wang et al., 2019).

When there are fewer choices, exhaustive search also called brute-force search is adopted to accomplish the optimization of evacuation routes, which is a very general problem-solving technique and algorithmic paradigm that consists of systematically enumerating all possible candidates for the solution and checking whether each candidate satisfies the problem's statement (Draganov Stojanovski, 2014), but it will be difficult or even impossible to get optimal results due to the huge amount of route combinations in large-scale problems (Uijlings et al., 2013). Thus the exhaustive search is typically used in small scale problems that do not have a large number of potential solutions. A modified exhaustive search method has been carried out to reduce computation costs (Chakrabarti and Kyriakides, 2008; Liu et al., 2016; Uijlings et al., 2013). Since the evacuation routes optimization problem does not have a large number of potential solutions, this paper employs the exhaustive search which is effective in small-scale situations to realize routing optimization. The Depth-First Search (DFS) algorithm, which is an exhaustive algorithm, has been employed to find all evacuation routes in this research.

The time-dependent concentration of toxic gas during dispersion is essential for planning evacuation routes. Simulation of accidental toxic gas leakage has been conducted since the early 1980s, and some numerical models and trails have been developed and used, such as Dense Gas Atmospheric Dispersion (DEGADIS), An Atmospheric Dispersion Model for Denser-Than-Air Releases (SLAB), Area Location of Hazardous Atmospheres (ALOHA), and Unified Dispersion Model (UDM) (Fan et al., 2016; Gerbec et al., 2017; Tauseef et al., 2011; Zhang et al., 2007). These models have been developed based on gas dispersion empirical formulas, though they are time-saving in computation, sometimes simulation results calculated by these models are not accurate enough to meet demands (Gavelli et al., 2008; Havens and Spicer, 2005; Qiao and Zhang, 2010). Whereas the computational fluid dynamics (CFD) simulation method has become one of the most appropriate ways to simulate toxic gas leakage and dispersion, and it has been verified by some experiments (Deng et al., 2012; Gavelli et al., 2008; Huang et al., 2012; Shen and Yu,

2008; Sun et al., 2013; Zhang et al., 2020). In this paper, based on the complete accident scenario set (CASS) (Zhang et al., 2019), time-dependent toxic gas concentration is obtained from CFD. Depending on two parameters: the concentration of toxic materials and the exposure time, the dose-response model has been widely used to evaluate the consequences of a toxic material exposure (Bagheri et al., 2016; Zhang and Chen, 2010).

In this paper, considering the time-dependent chlorine concentration, we combined dynamic dose response (DDR) model with CFD to evaluate the dynamic cumulative individual risk (CIR), and with the purpose of minimizing CIR, a MATLAB script based on the exhaustive search is developed to determine optimal evacuation routes.

The paper is organized as follows: Section 2 introduces the evacuation problem and sheds light on the results of the CFD simulation and the CIR model. Section 3 details the methodology of evacuation route planning. Conclusions are presented in Section 4. The nomenclature is shown in Table 1.

**Table 1.** Nomenclature

Nomenclature		
Acronym	CFD	Computational Fluid Dynamics
	CIR	Cumulative individual risk
	DFS	Depth First Search
	CASS	Complete accident scenario set
	DDR	Dynamic dose-response
	DEGADIS	Dense Gas Atmospheric Dispersion
	SLAB	An atmospheric Dispersion Model for Denser-Than-Air Releases
	ALOHA	Area Location of Hazardous Atmospheres
	UDM	Unified Dispersion Model
	IR	Individual risk
	HSE	Health and Safety Executive
	SIMPLE	Semi-Implicit Method for Pressure Linked Equations
Parameter	erf	Error function
	<i>m</i>	Toxic concentration index
	<i>A, B</i>	Constants depending on the types of toxic gases
	<i>f</i>	Exposure probability of evacuees to hazardous equipment
	<i>v</i>	Evacuation speed (m/s)
Variable	<i>t<sub>r</sub></i>	Response time of evacuees (s)
	<i>V</i> = {v <sub>1</sub> , v <sub>2</sub> , ..., v <sub>n</sub> }	Set of nodes
	<i>E</i>	Set of arcs
	v <sub>1</sub>	Starting node
	v <sub>n</sub>	Destination node
	i, j	Node i, j
	<i>x</i>	Abscissa of position (x, y) (m)
	<i>y</i>	Ordinate of position (x, y) (m)
	<i>D<sub>ij</sub></i>	Exposure dose when evacuating through arc (v <sub>i</sub> , v <sub>j</sub> )

$M_{ij}$	Decision variable
$k$	Leakage scenario
$R$	Complete route
$P_r$	Probit variable
$P$	Individual fatality probability
$P_k$	Occurrence probability of scenario $k$
$I$	Total number of leakage scenarios
$t$	Exposure time of evacuees (s)
$c_{ij}$	Concentration of toxic gas between time $t_i$ and $t_j$ (ppm)
$D(R)$	Exposure dose on route $R$
$n$	Total number of nodes
$t_i$	Time that evacuees enter arc $(v_i, v_j)$ (s)
$t_j$	Time that evacuees leave arc $(v_i, v_j)$ (s)
$IR_k(R)$	Individual risk under leakage scenario $k$ on route $R$
$CIR(R)$	Cumulative individual risk on route $R$ under all leakage scenarios

## 2. Material and methods

### 2.1. Problem description

Our first case study consists in modeling a Chlor-Alkali plant with a liquid chlorine preparation system, which is a sealed circulation system. The cyclic material is liquid and gas chlorine. The Chlor-Alkali plant has 6 workshops, 12 units, 46 production teams, and 326 workers. Chlorine is highly toxic. That means in case of severe leakage, workers' lives will be seriously threatened.

According to the layout of this chemical plant, an evacuation model is built to simulate the evacuation. The evacuation problem is a network flow problem with certain constraints. To emulate the flow

of evacuees, a graph  $\text{Graph} = (V, E)$  defined with sources and links is proposed to represent the network of the evacuation area.  $V$  denotes the set of nodes and  $E$  represents the set of arcs. Inside the chemical plant, nodes are used to describe the starting point, crossing roads and the destination point, and segment  $E$  show the links between nodes.

Node  $v_1$  near the leakage area is selected as the evacuation starting point. Similarly, node  $v_n$  in the safe area is selected as the destination node and all other nodes are intermediate nodes.

Restricted by the layout of roads and installations in the plant, where some nodes cannot be connected. This results in a directed evacuation network with 10 nodes and 15 arcs but first the evacuation area is simplified. The evacuation network topology is shown in Fig. 1.

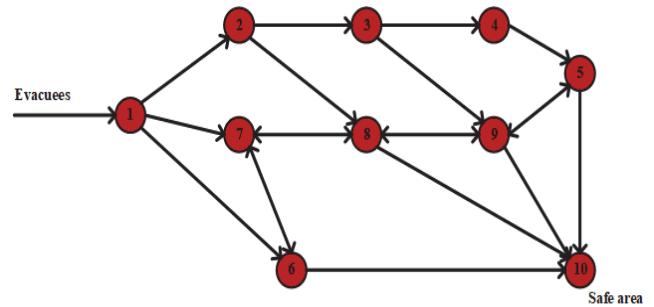


Fig. 1. The evacuation network topology

### 2.2. CFD simulation and outcomes

A previous CFD simulation is carried out to predict the leakage process of chlorine in this chemical plant (Li et al., 2018). The leakage and dispersion process, as well as the time-dependent concentration of chlorine are obtained from this simulation. The CFD simulation methodology is shown in Fig. 2, which will be described in the following.

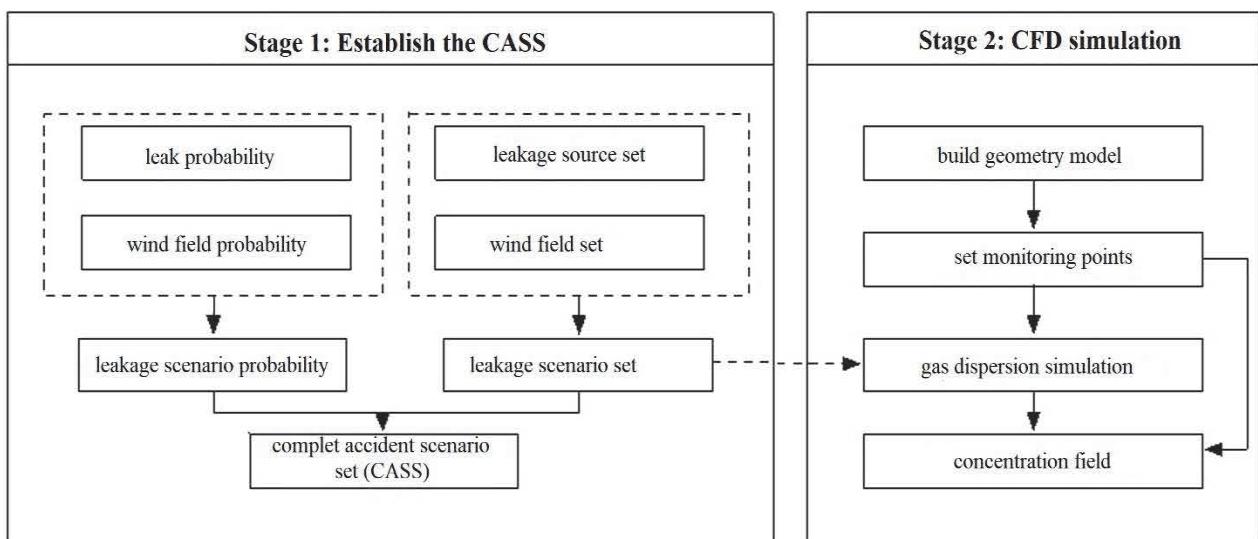


Fig. 2. The methodology of predicting leakage consequences by CFD

### 2.2.1 Establish the CASS

A former CFD simulation research has established the CASS to quantitatively represent the probability of leakage scenarios (Fu, 2017; Zhang, 2017). Wind field parameters according to local meteorological records and leakage sources based on the actual conditions of this factory are determined. Taking 8 different wind directions and 7 wind velocities in this area as parameters, the wind field set is established. The leakage source is identified by analyzing the liquid chlorine preparation system by experienced engineers, and four types of equipment: tank, liquefier, submerged pump, cylinder are determined.

Besides, four typical leakage apertures: small aperture, medium aperture, large aperture and catastrophic aperture are determined. The software LEAK 3.2, which uses a built-in failure database about chemical accidents in the world, is applied to predict the leakage probability of chlorine in different leakage sources with different leakage apertures (Fang et al., 2018).

By comparing the chlorine preparation system to similar facilities with available historical records in the database, the leakage probability can be calculated. Afterward, the leakage source set is built. According to the wind field set and leakage source set, the CASS built by 510 leakage scenarios is acquired. 88 leakage scenarios that account for over 90% of the total occurrence probability are screened out to reduce the computation costs.

### 2.2.2 CFD simulation

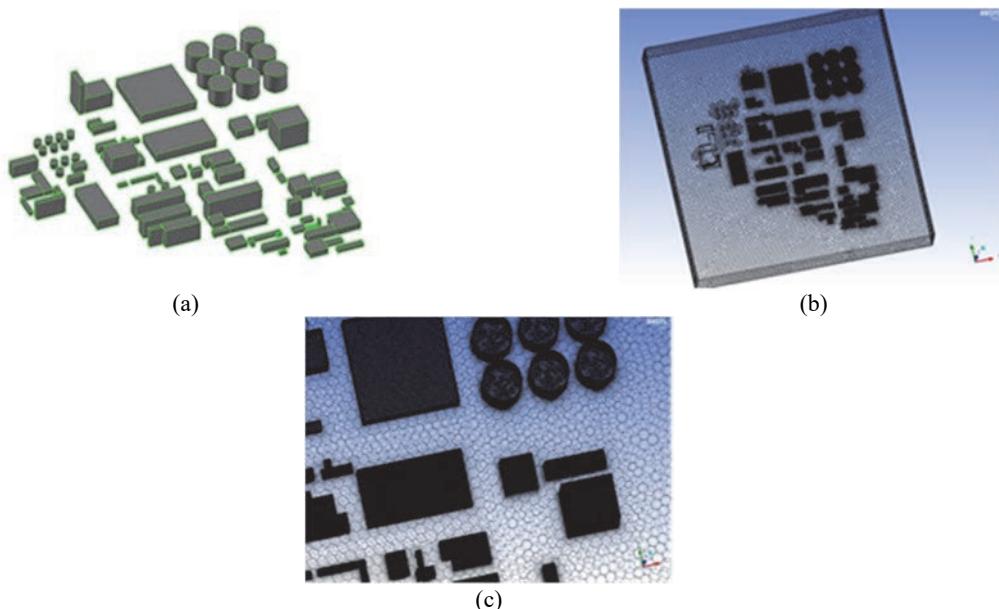
According to the detailed dimensions of the facility, the three-dimensional geometric model of the simplified chemical plant is established and meshed by the CFD preprocessor GAMBIT 2.4.6. And the grid is converted into the polyhedral grid after importing into CFD commercial code, Ansys-Fluent 14.5. The

geometry model and the mesh are presented in Fig. 3. According to the Chinese standard “Human dimensions of Chinese adults”, the mean shoulder height of Chinese male adults is 136.7 cm (CNSI, 1988). And Environmental Engineering Dictionary (Spellman, 2018) details the breathing zone is a hemisphere forward of the shoulders, centered on the mouth and nose, with a radius of 15.24 cm to 22.86 cm (6 to 9 inches). So 1.5 m above the ground is chosen as the height of monitor points to represent the actual height of human inhalation of chlorine. A total of 301 monitoring points is set up with a horizontal interval of 5 m to monitor the time-dependent chlorine concentration during the process of CFD solving, as shown in Fig. 4.

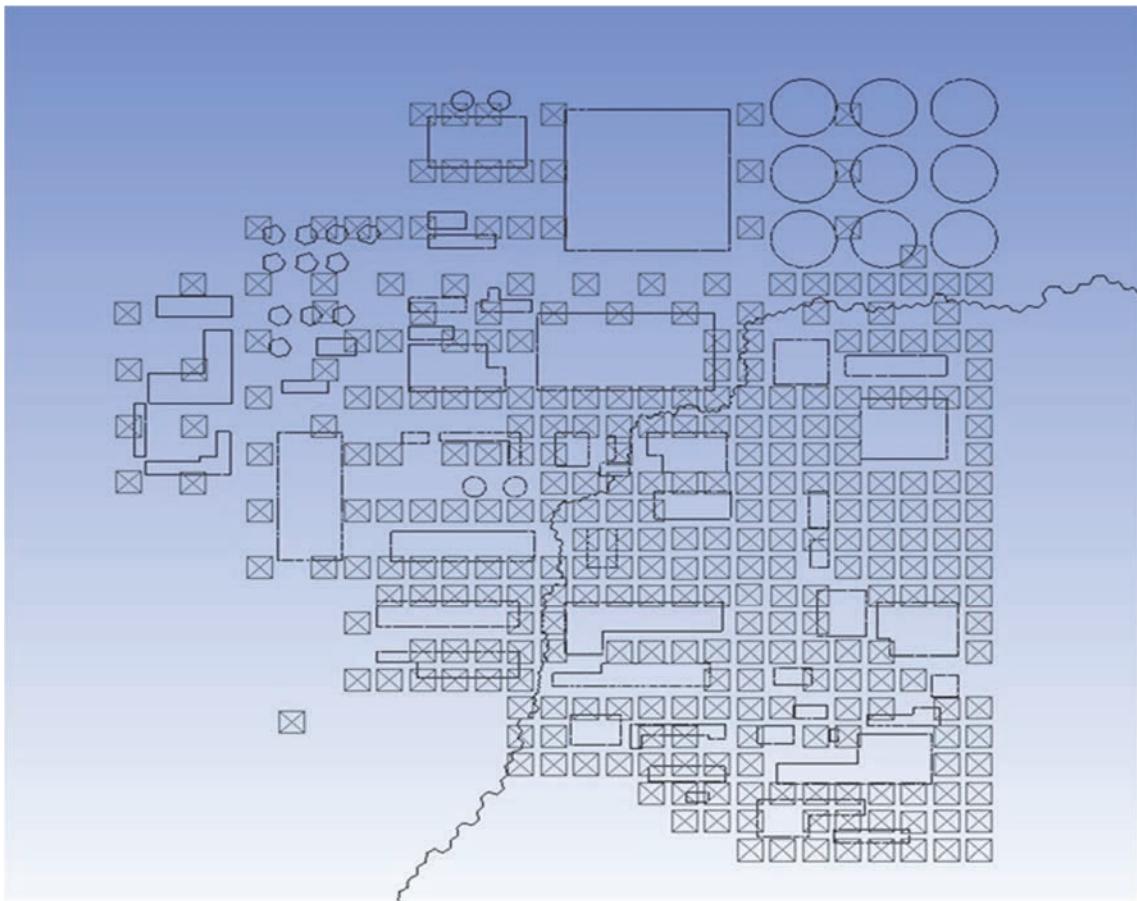
The concentration of chlorine can be recorded and exported as data files which contain important information for afterward calculations of toxic exposure doses. The simulation of chlorine leakage under 88 different leakage scenarios that screened out is implemented by Fluent.

The standard  $k$ -epsilon model is used for turbulent simulations. The Semi-Implicit Method for Pressure Linked Equations (SIMPLE) pressure-velocity coupling algorithm is applied to solve the pressure and velocity equations. The leakage duration time is 300 s with a time step of 2 s. The simulations are performed on a server with an Intel i7-4790 CPU (3.6 GHz and 32 GB RAM).

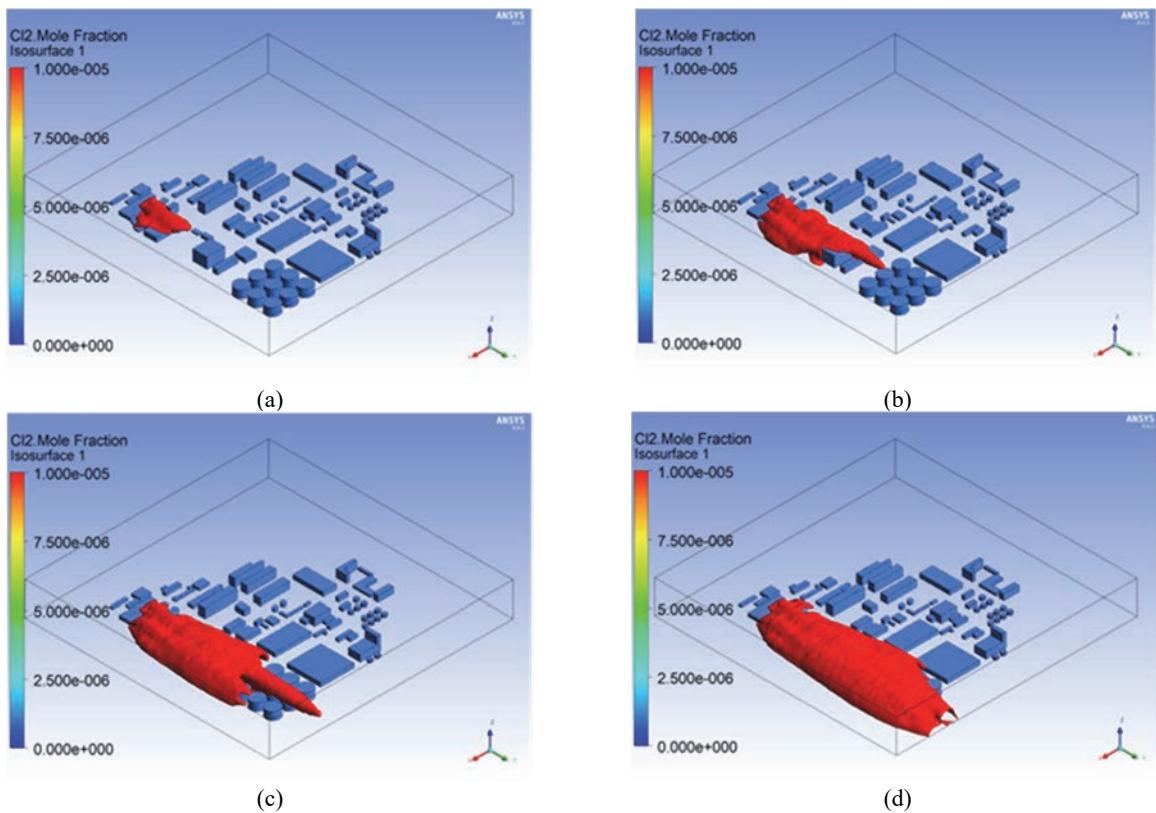
Chlorine concentration contours which are similar to those presented in Fig. 5 can be given through the CFD simulation of gas dispersion. By defining the concentration iso-surface of  $10 \times 10^{-6}$  mole fraction (10 ppm), the dispersion process of chlorine cloud is retrieved. The example shown in Fig. 5 is a medium aperture leakage of a tank in south wind, which illustrates the time sequence of chlorine concentration, the toxic gas cloud size and the affected area.



**Fig. 3.** (a) the three-dimensional geometry model, (b) (c) mesh generated for the model



**Fig. 4.** The distribution map of monitoring points (the symbol ‘ $\square$ ’ represents the monitoring point)



**Fig. 5.** An example of chlorine dispersion simulation results when a tank leaks at a medium aperture, south wind: (a) in 60 seconds, (b) in 120 seconds, (c) in 180 seconds, (d) in 240 seconds

## 2.3 CIR modeling

### 2.3.1 CIR calculation

In this paper, we use the definition of individual risk (IR) proposed by Health and Safety Executive (HSE) (Franks and Maddison, 2006) to judge the exposure risk. IR is defined as the risk that a typical user of a development is exposed to a dangerous dose or worse of toxic substance, heat or blast overpressure (Health and Safety Executive, 1989).

In the evacuation network defined by Graph=(V, E),  $V = \{v_1, v_2, \dots, v_n\}$  is the set of nodes corresponding to the intersections and  $E \subseteq V \times V$  is the set of arcs  $(v_i, v_j)$  corresponding to the roads. At the point  $(x, y)$ , the time-dependent concentration of chlorine can be obtained from simulation. Based on the evacuation speed, and the distance of arc  $(v_i, v_j)$ , the exposure dose  $D_{ij}$  when evacuating through arc  $(v_i, v_j)$  can be calculated by (Eq. 1).

$$D_{ij} = \int_{t_i}^{t_j} c_{ij}^m(x, y) dt \quad (1)$$

where  $m$  is the toxic concentration index which depends on the types of toxic gases.

And then, the exposure dose on route  $R$ ,  $D(R)$  can be illustrated by (Eq. 2).

$$D(R) = \sum_{i=1}^n \sum_{j=1}^n M_{ij} D_{ij} \quad (2)$$

$M_{ij}$  is a decision variable, which will be mentioned in the next section. After calculating the exposure dose under a certain leakage scenario, IR under leakage scenario  $k$  on route  $R$  can be calculated by Eqs. (3-5).

$$P_r = A + B \ln D(R) \quad (3)$$

$$P = 50 \left[ 1 + \frac{P_r - 5}{|P_r - 5|} \operatorname{erf} \left( \frac{|P_r - 5|}{\sqrt{2}} \right) \right] \quad (4)$$

$$IR_k(R) = f \times P_k \times P \quad (5)$$

In (Eq. 3),  $P_r$  is the probit variable,  $A$  and  $B$  are constants depending on the types of toxic gases. (Eq. 4) is the “probit function” (Georgiadou et al., 2010) used to calculate the individual fatality probability  $P$  on route  $R$ , where  $\operatorname{erf}$  is the error function. IR under leakage scenario  $k$  on route  $R$  can be calculated by (Eq. 5), which is a product of  $f$ ,  $P_k$  and  $P$ .  $f$  is the exposure probability of employees to hazardous equipment per year.

Considering IR on route  $R$  under all leakage scenarios, the CIR can be formulated by (Eq. 6).

$$CIR(R) = \sum_{k=1}^I IR_k(R) \quad (6)$$

where  $I$  is the total number of leakage scenarios. In this paper, based on the actual conditions of this chemical plant, we set the evacuation speed  $v$  as 2.5 m/s (Arampatzis et al., 1999). Then the exposure time  $t$  can be calculated based on the travel speed and the length of the arc which is the distance between 2 nodes. The time-dependent chlorine concentration can be obtained from CFD simulation results. Assume that after the gas detector alarms, the response time of the personnel is 0.16 s (Thompson et al., 1992). For chlorine,  $A$  is -5.3,  $B$  is 0.5,  $m$  is 2.75. Provided that working hours per year are 2000 hours based on the Labour Contract Law of the People's Republic of China (NPCSC, 2007), and according to the practice, the exposure time to hazardous equipment is 250 hours, then  $f$  is 0.125.  $P_k$  is the occurrence probability of leakage scenario  $k$ , which can be obtained from CASS.  $I$  is 88.

### 2.3.2 Modeling

In this paper, the objective is minimizing the CIR along a route. The linear programming formulation for evacuation route optimization is shown in Eqs. (7-10).

$$\begin{aligned} & \min CIR(R) \\ & \text{s.t.} \end{aligned} \quad (7)$$

$$\sum_{j=1, j \neq i}^n M_{ij} = 0 \quad i = n \quad (8)$$

$$\sum_{j=1, j \neq i}^n M_{ij} - \sum_{j=1, j \neq i}^n M_{ji} = \begin{cases} 1 & i = 1 \\ -1 & i = n \\ 0 & i \neq 1, i \neq n \end{cases} \quad (9)$$

$$M_{ij} \in \{0, 1\} \quad i, j = 1, 2, \dots, n \quad (10)$$

Constraints (Eqs. 8-10) determine a complete route (Gai et al., 2017), where,  $M_{ij}$  is the decision variable in this model, constraint (Eq. 10) is the 0-1 integer constraint, if arc  $(v_i, v_j)$  is included in route  $R$ ,  $M_{ij} = 1$ ;  $M_{ij} = 0$  means that arc  $(v_i, v_j)$  is not included in route  $R$ . Constraint (Eq. 9) limits that evacuees can't run backward after reaching the destination node, and constraint (Eq. 8) ensures  $R$  is a route from the starting node to the destination node without break.

## 3. Results and discussion

### 3.1. Find all possible routes by the DFS algorithm

The DFS algorithm is a recursive algorithm that uses the idea of backtracking, involving exhaustive searches of all the nodes by going ahead, is possible, else by backtracking. And it is an example of the brute-force search or exhaustive search (Coppin, 2004). First, the node  $v_1$  is visited. From  $v_1$ , any nearby node  $v_i$  can be visited. Then start from node  $v_i$ , and visit  $v_j$ , which has not been accessed before and is close by  $v_i$ . Continue this way until the destination

node  $v_n$  is reached. Based on the evacuation network topology of this chemical plant, the DFS algorithm is used in MATLAB R2018a to define the evacuation route collection. The methodology is shown in Fig. 6, and the route collection is shown in Table 2.

According to Fig. 1, the starting point is  $v_1$ , and the destination node is  $v_{10}$ , 15 evacuation routes are determined based on the directed evacuation network topology, and every route is connected by nodes according to Table 2.

### 3.2. Solving the risk model by MATLAB

Based on the actual conditions of this chemical plant and the exhaustive search, two sets of codes are implemented in MATLAB. The first one is the data extraction process, which is used to extract the time-dependent concentration from CFD simulation results, and form MAT files. The other one applies two IF loops to solve the CIR model. In detail the methodology looks like the following:

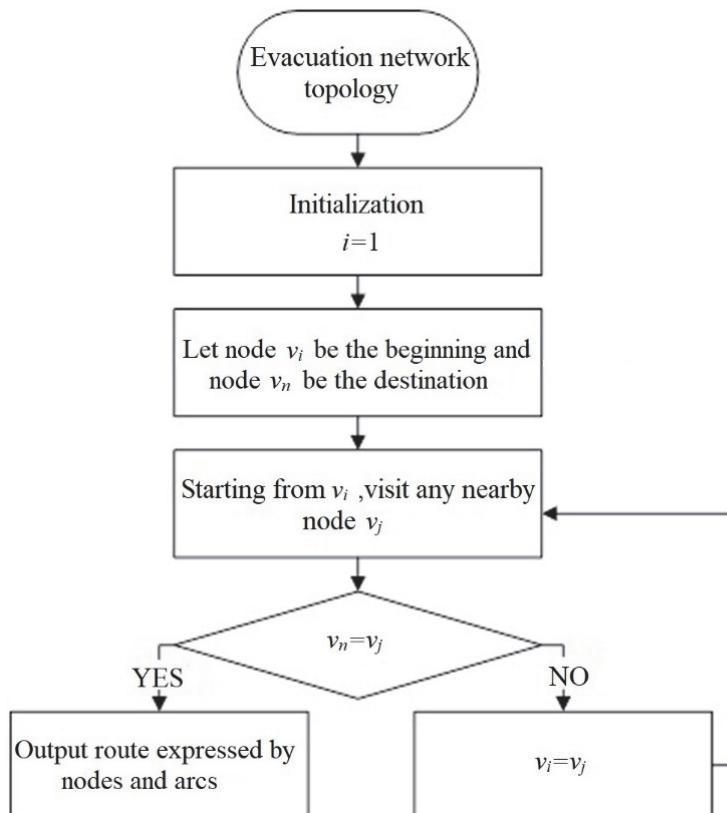
- Step1: Input data including time-dependent concentration at 301 monitoring points under 88 leakage scenarios, the routes presented by arcs and the occurrence possibilities of leakage scenarios. Let  $v_1 = v_i$ .
- Step 2: Start from  $v_i$ , search arc  $(v_i, v_j)$ ,  $i \neq j$  with  $j=1, 2, \dots, n$ . If arc  $(v_i, v_j)$  is included in route  $R$ , go to step 3, else, continue search.
- Step 3: Retrieve the time-dependent concentration at arc  $(v_i, v_j)$ , calculate the

corresponding dose. If  $v_j = v_n$ , go to step 4. Otherwise,  $v_j \neq v_n$ , let  $v_j = v_n$  and go back to step 2.

- Step 4: Calculate  $\sum_{k=1}^I IR_k$  on route  $R$  considering all leakage scenarios.

$CIR$  on every route is calculated by the MATLAB code. According to the assessment criteria of IR proposed by HSE, the routes can be classified as 3 types: broadly acceptable risk route ( $CIR$  less than  $10^{-6}$  per year), non-acceptable risk route ( $CIR$  larger than  $10^{-4}$  per year) and affordable risk route ( $CIR$  between  $10^{-4}$  to  $10^{-6}$  per year) (Franks and Maddison, 2006; Jonkman et al., 2003). The corresponding results are shown in Table 3.

From the results, with minimizing the  $CIR$  as the objective, it is obvious that route 10, 11, 12 have a higher risk than all other routes, thus they should be avoided when evacuating. The  $CIR$  of the other 12 evacuation routes are broadly acceptable according to the criteria of HSE and can be selected when liquid chlorine releases. The optimal routes among all evacuation routes are route 3 and 8. By analyzing all routes, it is found that these 3 routes of non-acceptable risk all include arc  $(v_1, v_6)$ , while all the other routes don't contain it. The arc  $(v_1, v_6)$  is firstly visited, the later arcs visited have little effect on the  $CIR$ . Though some routes like route 13 include point  $v_6$ , the risk is relatively low and acceptable. Thus, it can be given that evacuees will take more risks when they run through arc  $(v_1, v_6)$  and it should be avoided when evacuating.



**Fig. 6.** The methodology of DFS algorithm  
**Table 2.** The evacuation route collection defined by DFS

<b>Route</b>	<b>Nodes</b>
1	1→2→3→4→5→10
2	1→2→3→4→5→9→8→10
3	1→2→3→4→5→9→8→7→6→10
4	1→2→3→9→5→10
5	1→2→3→9→8→10
6	1→2→3→9→8→7→6→10
7	1→2→8→10
8	1→2→8→7→6→10
9	1→2→8→9→5→10
10	1→6→10
11	1→6→7→8→10
12	1→6→7→8→9→5→10
13	1→7→6→10
14	1→7→8→10
15	1→7→8→9→5→10

**Table 3.** CIR on each route

<b>Risk level</b>	<b>Route</b>	<b>Individual evacuation risk</b>	<b>Risk level</b>	<b>Route</b>	<b>Individual evacuation risk</b>
Broadly acceptable risk	1	2.41e-08		9	2.42e-08
	2	2.35e-08		13	2.06e-09
	3	4.63e-10		14	3.79e-08
	4	2.48e-08		15	3.79e-08
	5	2.41e-08	Non-acceptable risk	10	3.04e-02
	6	1.06e-09		11	3.04e-02
	7	2.42e-08		12	3.04e-02
	8	4.63e-10	Affordable risk	None	None

#### 4. Conclusions

This paper proposes a methodology for evacuation route optimization when accidental toxic gas release occurs within chemical plants, which can be applied in most chemical plants. Former CFD simulations have constructed the CASS and finished the simulation of chlorine leakage under 88 leakage scenarios. The purpose of this study is to systematically determine the evacuation routes and put forward the method of building and solving the optimization model. Applying the time-dependent concentration of chlorine that extracted from CFD simulation results, the DDR model and the probit function, the CIR can be systematically presented. Using the DFS algorithm, which is an example of the exhaustive search, all possible evacuation routes can be determined from the accident area to the safe area. With minimizing the CIR as the objective, a MATLAB script based on the exhaustive search is proposed to solve the optimization model. According to the IR criteria defined by HSE, the routes with unaccepted CIR as well as routes with broadly acceptable CIR can be finally determined, which can provide guidance for practical evacuation in chemical plants.

The exhaustive search i.e. the DFS algorithm, is effective when the problem does not have a huge number of potential solutions, but it may bring huge computation costs when the problem reaches a combinational explosion.

In future works, we should switch to heuristic algorithms like Swarm Intelligence Algorithm to solve problems with numerous potential solutions. Besides, the optimization model proposed in this paper does not take individuals' behaviors into account. But in practice, individual's behaviors do affect their evacuation process. For example, evacuation may be slower than expected due to panic, which will ultimately increase the CIR.

Moreover, it is generally required that the evacuation should go toward the upwind direction, while it is possible that a planned route is in the downwind direction under some specific gas release scenarios. Under this circumstance, choosing four routes of lower CIR concerning four different wind directions can be more beneficial for evacuees when making evacuation decisions. We are planning on looking into these points in the future to make the evacuation route optimization method more practical.

One of the future efforts of this work lies in using the heuristic algorithms and exhaustive search to solve the evacuation route optimization respectively, and compare their computation speed and final results. Then verify the effectiveness of exhaustive search when the problem does not have a huge number of potential solutions as well as the effectiveness of heuristic algorithms when the problem reaches a combinational explosion. Another future effort focuses on the improvement of optimization models, we will take the panic coefficient into account to make the model more practical.

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## References

- Arampatzis A., Brüggemann G.P., Metzler V., (1999), The effect of speed on leg stiffness and joint kinetics in human running, *Journal of Biomechanics*, **32**, 1349-1353.
- Aziz A., Farid M.M., Suryani E., (2017), *Floyd Warshall Algorithm with FIS Sugeno for Search Evacuation Route Optimization*, Int. Sem. on Application for Technology of Information and Communication, Semarang, Indonesia, 147-151, <http://doi.org/10.1109/ISEMANTIC.2017.8251860>.
- Bagheri M., Alamdar A., Davoudi M., (2016), Quantitative risk assessment of sour gas transmission pipelines using CFD, *Journal of Natural Gas Science and Engineering*, **31**, 108-118.
- Chakrabarti S., Kyriakides E., (2008), Optimal placement of phasor measurement units for power system observability, *IEEE Transactions on Power Systems*, **23**, 1433-1440.
- CNSI, (1988), Human Dimensions of Chinese Adults, *Chinese National Standardization Institute, Beijing, China*.
- Coppin B., (2004), *Artificial Intelligence Illuminated*, 1st Edition, Jones and Bartlett Publishers, Sudbury.
- CSB, (2015), Millard refrigerated services ammonia release, On line at: <https://www.csb.gov/millard-refrigerated-services-ammonia-release/>.
- Deng H., Chen G., Zhu Y., Fu J., Liu D., (2012), Simulation and experiment of gas leakage and dispersion in complex topography, *Journal of China University of Petroleum. Edition of Natural Science*, **36**, 122-126.
- Dou Z., Mebarki A., Cheng Y., Zheng X.P., Jiang J.C., Wang Y., Li Y., Li J.H., (2019), Review on the emergency evacuation in chemicals-concentrated areas, *Journal of Loss Prevention in the Process Industries*, **60**, 35-45.
- Draganov Stojanovski T., (2014), Performance of exhaustive search with parallel agents, *Turkish Journal of Electrical Engineering and Computer Sciences*, **22**, 1382-1394.
- Fan S., He T., An G., Liu Y., (2016), Numerical simulation of liquid hydrogen leakage diffusion, *Cryogenics*, **6**, 48-53.
- Fang Z., Guo H.L., Li G.F., Li W., (2018), Prediction of the leakage probability of equipment in liquid chlorine preparation system based on LEAK software, *Safety and Environmental Engineering*, **25**, 149-153.
- Franks A.P., Maddison T., (2006), A simplified method for the estimation of individual risk, *Process Safety and Environmental Protection*, **84**, 101-108.
- Fu G.R., (2017), *The research on chlorine leakage detection and evacuation route optimization*, MSc Thesis, Institute of China University of Geosciences, Wuhan, China.
- Gai W.M., Deng Y.F., Jiang Z.A., Li J., Du Y., (2017), Multi-objective evacuation routing optimization for toxic cloud releases, *Reliability Engineering and System Safety*, **159**, 58-68.
- Gai W.M., Du Y., Deng Y.F., (2018), Evacuation risk assessment of regional evacuation for major accidents and its application in emergency planning: A case study, *Safety Science*, **106**, 203-218.
- Gavelli F., Bullister E., Kytomaa H., (2008), Application of CFD (Fluent) to LNG spills into geometrically complex environments, *Journal of Hazardous Materials*, **159**, 158-168.
- Georgiadou P.S., Papazoglou I.A., Kiranoudis C.T., Markatos N.C., (2010), Multi-objective evolutionary emergency response optimization for major accidents, *Journal of Hazardous Materials*, **178**, 792-803.
- Gerbec M., Pontiggia M., Antonioni G., Tugnoli A., Cozzani V., Sbaouni M., Lelong R., (2017), Comparison of UDM and CFD simulations of a time varying release of LPG in geometrical complex environment, *Journal of Loss Prevention in the Process Industries*, **45**, 56-68.
- Havens J., Spicer T., (2005), LNG vapor cloud exclusion zones for spills into impoundments, *Process Safety Progress*, **24**, 181-186.
- Health and Safety Executive, (1989), *Risk Criteria for Land Use Planning in the Vicinity of Major Industrial Hazards*, H.M. Stationery Office, HSE Books, United Kingdom.
- Huang X.M., Guo Y.H., Peng S.N., Liao B., (2012), CFD simulation and experimental verification for indoor gas dispersion after an accidental leakage, *China Safety Science Journal*, **22**, 27-31.
- Jonkman S.N., Van Gelder P., Vrijling J.K., (2003), An overview of quantitative risk measures for loss of life and economic damage, *Journal of Hazardous Materials*, **99**, 1-30.
- Koca G.O., Dogan S., Yilmaz H., (2018), A multi-objective route planning model based on genetic algorithm for cuboid surfaces, *Automatika*, **59**, 120-130.
- Kou J.L., Xiong S.W., Fang Z.X., Zong X.L., Chen Z., (2013), Multiobjective optimization of evacuation routes in stadium using superposed potential field network based ACO, *Computational Intelligence and Neuroscience*, **2013**, 1-11.
- Li Q., Cai X., Wang X., Song Y., (2012), The environmental risk analysis of toxic gas leakage in Taiyuan coal chemistry industrial zone, *Acta Scientiae Circumstantiae*, **32**, 537-544.
- Li S., Chen G., (2012), Study on large-scale mixed emergency evacuation after disaster, *China Safety Science Journal*, **22**, 133-137.
- Li W., Zhang S.Q., Gao H.C., Zhou S.P., (2018), Arrangement optimization of leakage gas detector in liquid chlorine storage tank area, *Chemical Enterprise Management*, **19**, 86-88.
- Li X.X., (2009), On the optimal model of emergency evacuation decision-making in case of toxic chemicals leakage, *Journal of Safety and Environment*, **9**, 123-126.
- Liu M., Zhang F., Ma Y.L., Pota H.R., Shen W.M., (2016), Evacuation path optimization based on quantum ant colony algorithm, *Advanced Engineering Informatics*, **30**, 259-267.
- Qiao A., Zhang S., (2010), Advanced CFD modeling on vapor dispersion and vapor cloud explosion, *Journal of Loss Prevention in the Process Industries*, **23**, 843-848.
- Shen Y.T., Yu J.G., (2008), CFD simulation of hazardous gas dispersion after instantaneous release and safety analysis, *Journal of East China University of Science and Technology. Natural Sciences Edition*, **34**, 19-23.

- Spellman F.R., 2018, *Environmental Engineering Dictionary*, 5th Edition, Bernan Press, 94.
- Standing Committee of the National People's Congress, (2007), Labor Contract Law of the People's Republic of China, No. 65, On line at: [http://www.npc.gov.cn/zgrdw/englishnpc/Law/2009-02/20/content\\_1471106.htm](http://www.npc.gov.cn/zgrdw/englishnpc/Law/2009-02/20/content_1471106.htm).
- Sun B., Utikar R.P., Pareek V.K., Guo K.H., (2013), Computational fluid dynamics analysis of liquefied natural gas dispersion for risk assessment strategies, *Journal of Loss Prevention in the Process Industries*, **26**, 117-128.
- Tauseef S.M., Rashtchian D., Abbasi S.A., (2011), CFD-based simulation of dense gas dispersion in presence of obstacles, *Journal of Loss Prevention in the Process Industries*, **24**, 371-376.
- Thompson P.D., Colebatch J.G., Brown P., Rothwell J.C., Day B.L., Obeso J.A., Marsden C.D., (1992), Voluntary stimulus-sensitive jerks and jumps mimicking myoclonus or pathological startle syndromes, *Movement Disorders*, **7**, 257-262.
- Uijlings J.R.R., van de Sande K.E.A., Gevers T., Smeulders A.W.M., (2013), Selective search for object recognition, *International Journal of Computer Vision*, **104**, 154-171.
- Wang L., Wang R., Tao K., (2019), Research on capacity constrained evacuation route planning method in large-scale networks, *Science of Surveying and Mapping*, **44**, 235-241.
- Xi X.J., Shi C.L., Dai D.J., (2016), Assessment method of personnel evacuation safety based on dynamic toxic load, *Journal of Safety Science and Technology*, **12**, 170-173.
- Xiong M.Z., Zeng D.Z., Yao H., Li Y., (2016), *A Crowd Simulation based UAV Control Architecture for Industrial Disaster Evacuation*, IEEE Vehicular Technology Conf. Proc., IEEE, New York.
- Yuan F., Han L.D., (2009), Improving evacuation planning with sensible measure of effectiveness choices case study, *Transportation Research Record*, **2137**, 54-62.
- Yuan Y., Wang D., (2008), Route selection model in emergency evacuation under real time effect of disaster extension, *Journal of System Simulation*, **20**, 1563-1566.
- Zhang B., Chen G.M., (2010), Quantitative risk analysis of toxic gas release caused poisoning - A CFD and dose-response model combined approach, *Process Safety and Environmental Protection*, **88**, 253-262.
- Zhang B., Liu Y., Qiao S., (2019), A quantitative individual risk assessment method in process facilities with toxic gas release hazards: A combined scenario set and CFD approach, *Process Safety Progress*, **38**, 52-60.
- Zhang F., Liu M., Zhou Z., Shen W.M., (2013), *Quantum Ant Colony Algorithm-Based Emergency Evacuation Path Choice Algorithm*, Proc. of the 2013 IEEE 17<sup>th</sup> Int. Conf. on Computer Supported Cooperative Work in Design, Whistler, Canada, 576-580.
- Zhang J.H., Liu H.Y., Zhu R., Liu Y., (2017), Emergency evacuation of hazardous chemical accidents based on diffusion simulation, *Complexity*, **2017**, 1-16.
- Zhang J.W., An Y., Wei L.J., (2007), Review on atmospheric dispersion response to chemical models for emergency accidents, *China Safety Science Journal*, **17**, 12-17.
- Zhang X., (2017), *Risk Analysis of Leakage in Liquid Chlorine Process*, MSc Thesis, Institute of China University of Geosciences, Wuhan, China.
- Zhang W.T., Liu M.Q., Wang K.Y., Zhang F., Hou L., (2020), Numerical study on the gas leakage and dispersion at the street intersection of a building group, *CMES-Computer Modeling in Engineering and Sciences*, **123**, 1247-1266.
- Zheng X., Cai L., Zhang M., Jin L., Chen Y., (2019), Emergency evacuation path optimization model under multi-export conditions, *China Safety Science Journal*, **29**, 180-186.
- Zhou Y.F., Liu M., Zhang D.L., (2008), Area-wide emergency evacuation under toxic gas leakage, *Science Press Beijing*, **7**, 465-471.
- Zhu B., Yu X., Li Y., (2009), Research on influencing factors in the process of gas leakage and dispersion, *Chemical Engineering of Oil and Gas*, **38**, 354-358.